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Microwave Dielectric Property Retrieval from Open-Ended Coaxial Probe Response with Deep Learning

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Abstract—This work presents a technique for dielectric property retrieval through Debye parameter reconstruction from open-ended coaxial probe (OEC) response. Debye parameters were obtained with the application of a deep learning (DL) model to the reflection coefficient response of the OEC when terminated with a material under test. The OEC was modelled with the well-known admittance technique from 0.5 to 6 GHz with 20 MHz resolution. A dataset was generated using the admittance technique and obtained data was utilized to design the DL model. As part of the standard procedure, the dataset was separated to train, validate, and test parts by allocating the 80%, 10%, and 10% of the dataset to each section, respectively. Obtained percent relative error for Debye parameters were $1.86 \pm 3.01\%$, $3.33 \pm 9.52\%$, and $2.07 \pm 7.42\%$ for ϵ_s , ϵ_∞ and τ , respectively. To further test the constructed DL model, OEC responses were measured at the same frequency band when it was terminated with five different standard liquids, four mixtures, and a gel-like material. Reconstructed Debye parameters from the DL model were used to retrieve the complex dielectric properties and obtained results were compared with the literature data. Obtained mean percent relative error was ranging from 1.21 ± 0.06 to 10.89 ± 0.08 within the frequency band of interest.

Index Terms—Complex permittivity, Debye parameters, deep learning, open-ended coaxial probe, admittance model.

I. INTRODUCTION

MICROWAVE dielectric properties (DP), also referred to as complex permittivity, are critical system design parameters for the development of microwave diagnostic, imaging, treatment devices, and RF/microwave circuits. Therefore, inaccurate determination of the complex permittivity can render information resulting in poor system reliability. Based on the nature of the sample and frequency of interest different techniques can be employed to measure the DP. One such widely utilized technique is open-ended coaxial probe (OEC) method. The technique is used for the complex permittivity characterization of many different materials including but not limited to liquids, biological tissues, ice, and concrete [1], [2], [3], [4], [5], [6]. Provided that the full contact between the material under test (MUT) and the probe aperture is ensured, the method does not require strict sample preparation procedures. Additionally, the OEC technique is capable of performing wideband measurements of the MUTs complex

permittivity. While these advantages make the method a widely preferred tool for complex permittivity characterization, the OEC method is known to suffer from large measurement error. Commercially available probes report $\pm 5\%$ accuracy under ideal conditions [7]. It is reported that the measurement error can increase up to 30% [8]. Sources of error include but not limited to the mathematical approach, calibration degradation, sample heterogeneity. Since the DP are not measurable quantities, complex permittivities are derived from the other measurable quantities. Thus, the mathematical approach can be a major contributor to the measurement error. Addressing the mathematical approach can aid in the improvement of the measurement accuracy of the OEC technique.

In the OEC technique, reflected signals from the MUT are measured and converted to the complex permittivity. Different mathematical approaches have been implemented to retrieve the complex permittivity from measured reflection coefficients including the full-wave method and the equivalent circuit model [9], [10]. Full-wave analysis provides higher accuracy results for wideband but suffers from poor convergence and slow computing performances when processing large quantities of data. The equivalent circuit model provides faster computing; however, suffers from low accuracy and limited bandwidth [11], [12], [13].

In [14], an admittance model is proposed to mathematically represent the relationship between the MUT complex permittivity and the measured reflection coefficients at the probe aperture. Different solution approaches including the quasi-static approximation, Taylor Series approach, stochastic approach, and particle swarm optimization (PSO) were proposed in the literature to retrieve the complex permittivity from the admittance model [11], [15], [5], [16], [17], [18]. While iterative solution techniques can converge under certain constraints, such as being valid until a certain probe diameter, heuristic approaches are likely to be stuck in a local minima. Moreover, these methods have high computational complexity; for non-linear inverse estimation problems, they reach the solution either (i) in an iterative manner by means of linear or quadratic approximations of the problem at each step or (ii) solving the forward problem many times for each estimation. In contrast to these approaches, the deep neural network model proposed in this work offers a non-iterative and nonlinear solution of the inverse estimation problem by directly learning the non-linearity of the problem from the data generated with the admittance model [19]. Moreover, after the training phase, it needs only simple operations (summations, multiplications and activation function evaluations) and it does not require a

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solution of forward problem, which makes it easily adoptable in hardware. To this end, deep neural networks have been successfully employed in the literature for high dimensional microwave modelling, such as extracting the parameters of microwave filters [20]. Therefore, we believe that the deep neural networks can be utilized in similar nonlinear inverse problems in electromagnetic, to potentially improve the computation time and to reduce complexity of solution while enhancing the ease of implementation.

In this paper, we propose an alternative method to find Debye parameters which are used to represent the complex permittivity of materials for a wide frequency range. The Debye parameters are retrieved from the reflection coefficient of the probe through deep learning (DL) model designed by utilizing a synthetically generated dataset. The reflection coefficients were numerically calculated using the admittance model proposed in [14] and the designed DL model was then tested with the measurement data. Briefly, 276×17732 input dataset was generated corresponding to the 3×17732 output Debye parameters dataset. The scattering parameters of the probe were calculated between 0.5 - 6 GHz, with 20 MHz steps. The dataset was divided into three sections, 80% was used for training and 10% was used for validation. After the training procedure had ended, the remaining 10% of the dataset was used for testing. Obtained percent relative errors of the proposed model were $1.86 \pm 3.01\%$, $3.33 \pm 9.52\%$, $2.07 \pm 7.42\%$ for prediction of the Debye parameters ϵ_s (static dielectric permittivity), ϵ_∞ (dielectric permittivity at high frequencies), and τ (relaxation time constant), respectively. Finally, the trained deep learning model was tested with measurement data and it was found that the retrieved complex dielectric parameters had a percent mean relative error of approximately less than 10%.

In the literature, an artificial neural network model is proposed in [21] to compute the complex permittivity from the measured reflection coefficients for biomedical applications. In the proposed study [21], 102 experiment samples including standard liquids and biological tissues were measured in order to train, validate and test the neural network model. Prediction accuracy of $\pm 5\%$ was obtained for the complex permittivity. The study in [21] was limited with collected data from the experiments; therefore, the predictions of the trained neural network model was restricted. Composing a large dataset through measurements that include different materials, frequencies, and probes is labor intensive and costly. To the best of authors' knowledge, this work presents the first large scale study performed by designing a deep learning model using numerically generated data. Also, this work proposes to retrieve the Debye parameters from the reflection coefficient response of the OECP. The contributions of the paper and the added advantages are as follows:

- 1) One main contribution of this work is generation of data-set for training the deep neural network, which estimates the Debye parameters. In particular, unlike to [21], the input and output dataset was not measured but synthetically generated by means of a calibration procedure. Designing such procedures is an important topic for inverse electromagnetic estimation problems

[22], since it produces large amount of data required to train the deep learning model. Therefore, a more robust model is built in this work since a wide range of Debye parameters and reflection coefficients can be conveniently generated.

- 2) Since the probe is theoretically modelled, the proposed method provides design flexibility and ability to generate dataset for any desired probe with different dimensions.
- 3) Generating synthetic data shortens the time required for the collection of training data. For example, 276×17732 input dataset mentioned above was generated approximately in 50 mins on a computer with 192 GB RAM, $2 \times$ Intel(R) Xeon(R) X5690 3.47 GHz CPU. Furthermore, due to the features of deep neural networks, very large datasets can be easily trained using high-performance computing platforms such as GPUs.
- 4) Synthetic training approach proposed here is also flexible in data type and data production method. For instance, the dielectric permittivity model can be changed (Cole-Cole, Debye or multipole Debye) simply by using the target model for complex permittivity calculation or the simulation method can be different (instead of using the admittance model [14], numerical electromagnetic software such as HFSS or CST can be employed).
- 5) Different from the verification of previously proposed dielectric retrieval methods, which is usually performed by measuring few standard liquids, this work presents a statistical verification of the DL-based dielectric property retrieval technique both with synthetically generated and measured data.

The remainder of this paper is organized as follows: Section II-A presents the admittance model. Process for synthetic dataset generation is explained in section II-B. Measurement procedure and the experimental setup are given in section II-C. The design of the deep learning model is presented in section II-D. Results are given in section III and conclusions are drawn in section IV.

II. MATERIAL AND METHODS

In the following section, we first present the theoretical background for retrieving the Debye parameters from the reflection coefficient using the OECP and admittance model. Second, based on the theoretical model, the dataset was generated to train, validate, and test the deep learning model. Furthermore, to test the deep learning model with measurement data, experiments were conducted to acquire the reflection coefficients of standard liquids, mixtures, and a gel-like material. Finally, the design process for the deep learning model to retrieve the Debye parameters from the reflection coefficient is given in detail.

A. Admittance Model for The Open-Ended Coaxial Probe

The configuration of the OECP consists of two concentric cylindrical conductors with a dielectric material placed between the conductors. When the OECP is utilized to obtain the dielectric properties of a MUT, the relation between the complex permittivity of MUT and the admittance of the probe

is given by the classical admittance model as shown below in equation (1) [14]:

$$\frac{Y(\epsilon)}{Y_0} = \frac{ik_0^2\epsilon_c}{k_d \ln(b/a)} \int_0^\infty \frac{[J_0(\zeta a) - J_0(\zeta b)]^2}{\zeta \sqrt{\zeta^2 - k_0^2\epsilon_c}} d\zeta \quad (1)$$

where $Y(\epsilon)$ represents admittance of the probe when terminated with MUT, Y_0 is the probe characteristic admittance, a and b represent the inner and outer radius of the conductors, respectively. $J_0(\cdot)$ is the first order Bessel function, k_d denotes the wave number of the dielectric material (between conductors) and k_0 represents the free space wave number. ϵ_c is the complex dielectric permittivity of the MUT which can be expressed in terms of Debye parameters:

$$\epsilon_c(\omega) = \epsilon_\infty + \frac{\epsilon_s - \epsilon_\infty}{1 + i\omega\tau} \quad (2)$$

where ω represents the angular frequency, ϵ_s is the static constant, ϵ_∞ is the infinite frequency dielectric constant and τ is the characteristic relaxation time. Debye parameter equation 2 can be used for generating the complex dielectric constant. The admittance of the probe can then be derived from the equation 1.

As result of the impedance difference between the reference medium and the MUT, the reflection coefficient Γ at the probe's aperture can be expressed in terms of the ratio between the admittance of the MUT $Y(\epsilon)$ and the probe characteristic admittance Y_0 :

$$\frac{Y(\epsilon)}{Y_0} = \frac{1 + \Gamma}{1 - \Gamma} \quad (3)$$

From the equation 3 corresponding reflection coefficient can be derived. However, it should be noted that this represents the calculated reflection coefficient and does not correspond to a measured reflection coefficient. For a measured reflection coefficient, there is a need to adjust the reference plane of measurement through calibration in order to utilize equation 3 for measurements. Therefore, a calibration procedure is required to acquire the reflection coefficient (Γ_c) at the probe's aperture. Please note that Γ_c will be used to denote the calibrated reflection coefficient throughout this paper. Suppose, ρ represents the reflection coefficient obtained from the MUT and ρ_1, ρ_2, ρ_3 are the reflection coefficients corresponding to three known material terminations. The reflection coefficient at probe's aperture (Γ_c) can be obtained from the measured reflection coefficients $\rho, \rho_i, (i = 1, 2, 3)$ with the following expression:

$$\Gamma_c = \frac{\rho - S_{11}}{\rho S_{22} + S_{12}S_{21} - S_{11}S_{22}} \quad (4)$$

where S_{11}, S_{12}, S_{21} and S_{22} represent the unknown scattering parameters of the network [8], which can be evaluated with the subsequent equations:

$$S_{11} = \frac{\Gamma_1\Gamma_2\rho_3(\rho_1 - \rho_2) + \Gamma_1\Gamma_3\rho_2(\rho_3 - \rho_1) + \Gamma_2\Gamma_3\rho_1(\rho_2 - \rho_3)}{\Gamma_1\Gamma_2(\rho_1 - \rho_2) + \Gamma_1\Gamma_3(\rho_3 - \rho_1) + \Gamma_2\Gamma_3(\rho_2 - \rho_3)} \quad (5)$$

$$S_{12}S_{21} = \frac{(\rho_1 - S_{11})(1 - S_{22}\Gamma_1)}{\Gamma_1} \quad (6)$$

$$S_{22} = \frac{\Gamma_1(\rho_2 - S_{11}) + \Gamma_2(S_{11} - \rho_1)}{\Gamma_1\Gamma_2(\rho_2 - \rho_1)} \quad (7)$$

where Γ_1, Γ_2 , and Γ_3 are the calculated reflection coefficients of the known materials using equations (1) and (3). For a measurement from a MUT, once the scattering parameters are calculated from the given expressions above, equation 4 is used to calculate the reflection coefficient at the aperture.

B. Procedure for Obtaining the Deep Learning Dataset

In this section, the expected reflection coefficient (Γ) due to material's complex permittivities (ϵ_c) is calculated using the admittance model. To do so, Debye parameters corresponding to a wide range of complex permittivity values were systematically generated. Note that the Debye parameters are frequently used for mathematical modelling of frequency dispersive complex permittivity. The theoretical relation between the Debye parameters and reflection coefficient at the probe's aperture can be expressed using equations (1), (2) and (3). Using any given set of Debye parameters ($\epsilon_s, \epsilon_\infty, \tau$), the corresponding reflection coefficient (Γ) at the probe's aperture can be directly calculated. The following steps were implemented to generate the required dataset. First, Debye parameters were generated by varying ϵ_s from 5 - 120 units, ϵ_∞ from 1 - 10 units, τ from 20 - 180 ps with constant step size of $\frac{5}{\sqrt[3]{2}}, \frac{1}{\sqrt[3]{2}}$ and $\frac{4}{\sqrt[3]{2}}$, respectively. The step sizes were determined by trial and error. In this trial and error process the point that we noticed is to divide the output space (the space spanned by $\epsilon_s - \epsilon_\infty - \tau$) into equal pieces as much as possible in all three parameters. Next, generated Debye parameters were combined and a total of 17748 Debye parameter sets were obtained. Then, the complex dielectric properties were produced using Debye parameter sets. The frequency range was selected from 0.5 to 6 GHz with 20 MHz resolution (a total of 276 frequency points). Synthetically generated complex permittivity values were then placed in equation (1) to obtain the corresponding admittance. It should be noted that the dimensions of the probe (a and b in equation (1)) were chosen based on the commercially available Dielectric Assessment Kit (DAK). The outer radius of the probe (a) is 1.75 mm and inner radius (b) is 0.465 mm [23]. Finally, equation (3) was used to obtain the reflection coefficient. Through the application of this process, a dataset composed of reflection coefficients and corresponding Debye parameters was obtained. The dimensions of the dataset were 276×17748 (Γ) matrix (input of the deep learning model) corresponding to 3×17748 Debye parameters (output of the deep learning model).

C. Experimental Setup and Protocol for Reflection Coefficient Measurements

Since the deep learning algorithm is modelled based on the generated theoretical data, it is critical to evaluate the model's performance with real measurements. Therefore, an

Fig. 1. Experimental setup and its components. (a) Experiment setup 1. N5230A PNA Series Network Analyzer, 2. RF cable, 3. sample: standard liquid and 4. EXTECH thermometer, (b) DAK 3.5 probe, and (c) mechanical calibration kit.

Fig. 2. Comparison of theoretically calculated reflection coefficient of formamide based on Debye parameters [24] and calibrated reflection coefficient obtained from measurements.

experiment setup shown in Fig. 1 (a) was used to collect the reflection coefficient responses of the probe with standard pure liquids. The experiment setup consisted of N5230A PNA Series Network Analyzer (Santa Clara, CA, USA) and the commercial Speag DAK 3.5 mm-diameter open-ended coaxial probe (Zurich, Switzerland), shown in Fig. 1 (a) and (b). The frequency range of the analyzer was set from 0.5 to 6 GHz with 20 MHz increments; that is, 276 frequency points consistent with the synthetically generated data. An IF bandwidth of 10 Hz was selected to reduce the error due to noise. The analyzer and probe were connected via an RF cable. Before connecting cable to the probe, the Agilent 85033E 3.5 mm standard mechanical calibration kit (Santa Clara, CA, USA), as seen in Fig. 1 (c), was used for RF calibration with the aim to transfer the measurement reference plane to the end of the cable.

Obtaining the reflection coefficient for any MUT requires the calibration of the probe. The standard protocol for calibrating the OECP is a three-step process (open circuit, short circuit and distilled water). Probe calibration procedure for obtaining the reflection coefficient Γ_c is given in section II-A. To apply the given procedure in the section, measured reflection coefficients for the MUT (ρ) and the reflection coefficients of three known materials (ρ_1, ρ_2, ρ_3) were collected. The ρ_1, ρ_2, ρ_3 were measured by allowing the probe to radiate in free space (Open), terminating the probe's aperture with a copper strip (Short) and with a reference material (distilled water) respectively. The measured pure materials were DMSO, ethanol, ethylene glycol, formamide and methanol. The temperatures of the materials were $17.8 \pm 0.2^\circ\text{C}$ at the time of the measurement. The mixtures were prepared via volume fractions: formamide (90%)-1-butanol (10%), formamide (70%)-1-butanol (30%), DMSO (23%)-ethanol (77%) and DMSO (54%)-1-butanol (46%) at temperatures of $24.5 \pm 0.9^\circ\text{C}$. Apart from the liquids/solutions, a gel-like material was prepared by mixing deionized water (15 ml) and triton X-100 (15 ml) at 23.5°C . Each measurement, (3 reflection coefficients for calibration step and the measurement of the samples) were repeated five times for statistical verification purposes. As an example of the consistency between the theoretical calculation and calibration, Fig. 2 depicts the comparison of the theoretically calculated Γ and the Γ_c obtained from the calibrated reflection coefficient of formamide. From this figure, it can be concluded that the measured and theoretically generated data from the Debye parameters of formamide are in good agreement.

D. Deep Learning Model Design

Recently, many different studies have adopted deep learning to model nonlinear input-output relationships. This work presents the design of a deep neural network with 5 hidden layers as seen in Fig. 3. The inputs of the network were the real and imaginary parts of the reflection coefficients. As described in section II-B, the input dataset was generated through the admittance model [14]. Before training the network, as a constraint, generated data with $\epsilon_s < \epsilon_\infty$ were omitted from the data set since it is known that most materials possess $\epsilon_s > \epsilon_\infty$ property. This approach shrank the dataset to 276×17732 reflection coefficients as input data and 3×17732 Debye parameters as the corresponding output data. Next, the dataset was divided into three sections, 80% was used for training and 10% was used for validation. After the training procedure was ended, the remaining 10% of the synthetically generated dataset was used for testing the designed network. Further, validation of the designed network was performed with the measured reflection coefficient data collected from a number of well-known liquids. As explained in section II-C, in order to collect a measurement dataset compatible with the synthetically generated data, reflection coefficients of the commercially available DAK probe were measured between 0.5 to 6 GHz, with steps of 20 MHz. Thus, the obtained number of input parameters and the frequencies were consistent with the synthetic dataset.

The strategy of setting the neural network can be summarized as follows:

- 1) Normalize the output parameters with respect to its maximum value. For this study, ϵ_s , ϵ_∞ and τ were normalized by 120, 10, and 180 ps, respectively. This approach was applied in order to increase the numerical stability of training.
- 2) Number of inputs is determined by the number of frequencies for which the measurements are performed. (For this study, the number of inputs was 2×276 since the input parameters are complex numbers.) The number of outputs is the number of parameters that is to be extracted. Note that in this work, the dielectric properties (DP) is mathematically represented with the Debye equation and the number of Debye parameters is three; thus, the number of outputs were three. The design can be started with a single hidden layer, whose size is determined as B^{p_i} , $B, p_i \in N$ (i.e. integer powers of an integer) where i is the order of the related layer. In this study, $B = 2$ and we started with $p_1 = 7$.
- 3) Assume that there are L many hidden layers, let the training error for this case is $E_{t,L}$ and validation error for this case is $E_{v,L}$. If $E_{t,L} \approx E_{v,L}$ then increase the number of free parameters of neural network either by choosing $p_L := p_L + 1$ or by setting $p_{L+1} > 0, p_{L+1} \in N$.
- 4) If $E_{t,L+1} \approx E_{v,L+1} < E_{t,L} \approx E_{v,L}$, then go step 3. If $E_{t,L+1} < E_{t,L}$ but $E_{v,L+1} \approx E_{v,L}$ then the neural networks start to overfit the data; thus, go to the previous state and choose the final design with L layers.

Following the guidelines given above, the deep neural network model shown in Fig. 3 was designed. Please note that using batch normalization (BN) and Relu layer (ReLU) after each dense layer (DN), improves the model. Thus, after each dense layer, these two blocks were applied to the data subsequently. Finally, a regression layer (RL) was applied. The given model was trained on GPU using Matlab's Deep Neural Network Toolbox on a computer with 32 GB RAM, 16 GB Intel(R) UHD Graphics 630 GPU, 2.6 GHz CPU. In the training, maximum of 200 epochs were applied to the model and Adam optimizer was used with least mean square error cost function. The training lasted approximately 10 mins and at the end of training the model had a loss of 0.02 for both training and validation data, indicates that the model did not overfit. Finally, to further show that the model can represent the nonlinear relationship between reflection coefficients and Debye parameters, test data (10% of the synthetic dataset) was processed by the trained network. For each case, the predicted Debye parameters were compared with the actual values and the percent relative error for each parameter was computed ($\frac{|Predicted - Exact|}{|Exact|} \times 100\%$). There were approximately 1700 sample in the test data and the histograms of percent relative error for each parameter are given in Fig. 4. Additionally, the mean and standard deviation of the percent relative errors of the test data are given in Table I. As can be seen from these results, the designed model can accurately determine the Debye parameters.

Fig. 3. Designed deep learning model with dense layer (DN), batch normalization (BN), Relu layer (ReLU) and regression layer (RL) for predicting Debye parameters from reflection coefficients.

Fig. 4. Histograms of percent relative errors for each output parameter (ϵ_s , ϵ_∞ and τ) obtained for 1700 samples in the test set (10% of the synthetic dataset).

III. RESULTS AND DISCUSSION

To further test the optimized deep learning model with measured data, a dataset was generated by using 5 standard liquids; namely, dimethyl sulfoxide (DMSO), ethanol, ethylene glycol, formamide, and methanol; and 4 mixtures. To compose the dataset, 5 reflection coefficient measurements with the commercially available DAK probe were collected from each of the liquids/mixtures, and the calibration standards; that is, open, short and distilled water. Then, 5 measurements for each material were combined with the calibration (open+short+water+material) to obtain a total of 625 different measurement. Thus, the obtained test datasets generated from experiments were composed of 5×625 measurements for standard liquids and 4×625 measurements for mixtures. Apart from these two dataset, the deep learning model was tested with a gel-like material with the same data collection process.

The first dataset (5×625) was fed to the optimized deep neural network and the mean of the obtained network outputs;

TABLE I
THE MEAN AND STANDARD DEVIATION OF THE PERCENT RELATIVE ERRORS FOR DEBYE PARAMETERS (ϵ_s , ϵ_∞ AND τ) OF THE TEST SET (10% OF THE SYNTHETIC DATASET)

Debye parameters	Mean (%)	Std dev. (%)
ϵ_s (units)	1.86	3.01
ϵ_∞ (units)	3.33	9.52
τ (ps)	2.07	7.42

TABLE II
COMPARISON OF DEBYE PARAMETERS GIVEN IN LITERATURE AND MEAN OF THE RETRIEVED DEBYE PARAMETERS FROM THE DESIGNED NEURAL NETWORK (NN) FOR STANDARD LIQUIDS. MPE±SPE FOR THE CALCULATED COMPLEX PERMITTIVITY (ϵ_c) FROM RETRIEVED DEBYE PARAMETERS WITH RESPECT TO LITERATURE VALUES FROM 0.5 TO 6 GHz

Standard Liquids	ϵ_s (units)		ϵ_∞ (units)		τ (ps)		ϵ_c MPE±SPE (%)
	Ref.	NN-results	Ref.	NN-results	Ref.	NN-results	
Dimethyl sulfoxide [25]	47.13	46.81	6.8	4.98	21.6	19.86	1.21±0.06
Ethanol [26]	25.07	22.82	4.2	4.00	143.24	150.22	10.89±0.08
Ethylene Glycol [27]	35.85	37.34	4.23	4.79	99.62	115.14	6.08±0.02
Formamide [24]	111.8	109.23	6.9	5.26	42.00	42.9	3.68±0.03
Methanol [26]	33.64	37.01	5.7	4.94	53.05	57.21	8.53± 0.02

Fig. 5. Comparisons of calculated complex permittivities from the retrieved mean of Debye parameters and literature values of complex permittivities for five standard liquids: dymethyl sulfoxide, ethanol, ethylene glycol, formamide and methanol.

Fig. 6. The calculated E_{single} of eq.(8) of deep learning model by testing over 625 measurements for each standard liquid.

TABLE III

COMPARISON OF DEBYE PARAMETERS GIVEN IN LITERATURE AND MEAN OF THE RETRIEVED DEBYE PARAMETERS FROM THE DESIGNED NEURAL NETWORK (NN) LIQUID MIXTURES. $MPE \pm SPE$ FOR THE CALCULATED COMPLEX PERMITTIVITY (ϵ_c) FROM RETRIEVED DEBYE PARAMETERS WITH RESPECT TO LITERATURE VALUES FROM 0.5 TO 6 GHz

Liquid Mixtures (Vol. frac. %)	ϵ_s (units)		ϵ_∞ (units)		τ (ps)		ϵ_c
	Ref.	NN-results	Ref.	NN-results	Ref.	NN-results	
Formamide (90) & 1-Butanol (10) [28]	101.0	100.69	5.0	2.64	41.1	43.9	5.9 ± 0.18
Formamide (70) & 1-Butanol (30) [28]	79.0	78.14	4.9	3.29	58.3	56.95	1.75 ± 0.05
* DMSO (23) & Ethanol (77) [29]	29.4	29.35	4.7	4.4	80.8	53.6	8.9 ± 0.06
** DMSO (54) & 1-Butanol (46) [29]	34.1	33.83	4.3	4.43	51.5	39.11	4.83 ± 0.02

* The parameter of β equals 0.77 in Debye equation [29].

** The parameter of β equals 0.84 in Debye equation [29].

Fig. 7. Comparisons of calculated complex permittivities from the retrieved mean of Debye parameters and literature values of complex permittivities for three liquid mixtures: formamide (90%) & 1-butanol (10%), formamide (70%) & 1-butanol (30%), DMSO (23%) & ethanol (77%) and DMSO (54%) & 1-butanol (46%).

Fig. 8. The calculated E_{single} of eq.(8) of deep learning model by testing over 625 measurements for each liquid mixture.

that is, mean Debye parameters corresponding to the dataset and literature values for five standard liquids are listed in Table II. Furthermore, the complex permittivity was computed from the retrieved Debye parameters using equation (2). The mean of percent relative error (MPE) and standard deviation of percent relative error (SPE) for the calculated complex permittivity from the retrieved Debye parameters are also given in Table II. The MPE was calculated from 0.5-6 GHz using the equation of:

$$E_{single} = \frac{\sum_{Freq} \frac{|Predicted-Exact|}{|Exact|}}{276} \times 100 \quad (8)$$

$$MPE = \frac{\sum_{Measurements} E_{single}}{625} \quad (9)$$

where ‘Predicted’ is the complex permittivity calculated from the Debye parameters acquired from the deep learning neural network model and ‘Exact’ is the complex permittivity computed using Debye parameters obtained from the literature. Similarly, the SPE is calculated as:

$$SPE = \frac{\sum_{Measurements} (E_{single} - MPE)^2}{625} \quad (10)$$

As seen in Table II, all MPEs are below 11%. Moreover, the SPEs for complex permittivity is below 0.08 units, which demonstrates that the deep learning model is robust enough to predict Debye parameters from reflection coefficients. In Fig. 5, a comparison of real (ϵ') and imaginary (ϵ'') parts of the complex permittivity calculated from the retrieved neural network Debye parameters and literature values are shown for five standard liquids from 0.5 to 6 GHz. To further investigate the accuracy of the deep learning model, the histograms for E_{single} of eq.(8) is given in Fig. 6. The maximum E_{single} was 11.1% for ethanol and the minimum E_{single} was 1.1% DMSO.

The second test dataset (4×625) includes the prepared mixtures. The mean of the estimated Debye parameters from neural network (NN) corresponding to the dataset and the literature values are listed in Table III. Also, in the last column of Table III, the MPE and SPE for the calculated complex permittivity from the retrieved Debye parameters is given. The results from Table III indicate that the obtained MPEs for all the mixtures are below 8.9%. Furthermore, the SPEs for complex permittivity is below 0.18 units. Comparison of the real (ϵ') and the imaginary (ϵ'') parts of the complex permittivity, which are computed from the retrieved Debye parameters and the literature, are shown in Fig. 7. The histograms E_{single} in complex permittivity for each mixture are given in Fig. 8. The maximum E_{single} for the calculated complex permittivity was 9.05% for the DMSO and ethanol mixture (volume ratio 2.3:7.7) and the minimum E_{single} obtained from the formamide and 1-butanol mixture (volume ratio 7:3) is 1.6%. As seen from the histograms, the error of prediction from the deep learning model has differed in a small range for each sample.

The obtained results are an indication that the proposed approach is robust and can be used to retrieve the dielectric properties of materials with the OECF technique. When this study is compared with the previously reported work in the

literature, to the best of authors’ knowledge, only one reported work carried out a study utilizing NN to retrieve complex permittivity with OECF response [21]. However, the reported study only used measurements; therefore, train and test data were restricted with the measurements and availability of the materials. Also, in [21], the complex permittivity values of methanol were calculated from 0.5 to 5 GHz frequency range from three samples. The obtained real and imaginary values for methanol at 2.45 GHz were approximately 24 and 15 units, respectively. The computed real and imaginary values from the Debye parameters of methanol retrieved from the deep learning algorithm proposed in this work at 2.46 GHz are 23 and 15.9 units, respectively. To further expand the comparison, a gel-like solution containing 15 ml Triton X-100 and 15 ml de-ionized water was prepared. At 2.45 GHz, [21] reported 35 and 8 units for real and imaginary parts of DP, respectively. In this work, the retrieved real and imaginary DP values from the trained NN at 2.46 GHz are 33.4 and 10.4 units, respectively. It should also be noted that, unlike [21], our work provides statistical analysis of 625 different combinations of methanol measurements.

In [25], the traditional approach for dielectric property characterization with iterative solution techniques was implemented. Furthermore, the Debye parameters of DMSO between 30 MHz and 5 GHz frequency band were reported with approximately 95% confidence level using linear interpolation via Monte Carlo modelling. The calculated MPE between obtained results in this work and [25] is 1.21 ± 0.06 for DMSO. As seen in Table II, the maximum error was observed in the complex permittivity of ethanol. Instead of the single-pole Debye (3 parameters), the Debye- Γ (4 parameters) can potentially offer a more suitable relaxation equation for ethanol as mentioned in [25]. In [27], the measurement of ethylene glycol was performed using the transmission line (TL) approach from 0.3 to 3 GHz. The Debye parameters were calculated from the complex permittivity by solving a system of nonlinear equations using MATLAB’s *fsolve* function. The calculated Debye parameters for ethylene glycol differ from the work in [27] as much as 1.51 units, 0.56 units and 15.52 ps for ϵ_s , ϵ_∞ and τ , respectively. These differences can be due to the different approaches used in obtaining the Debye parameters. In [24], the complex permittivity of formamide was measured from 10 MHz to 70 GHz frequency range and the best fit was represented by a single-Debye type dispersion. As seen in Table II, the retrieved Debye parameters difference in [24] and this work is 2.57 units, 1.64 units and 0.9 ps for ϵ_s , ϵ_∞ and τ , respectively. In [28], formamide and 1-butanol were mixed with different volume fractions. The measurements were taken over the frequency range of 0.2 to 13.5 GHz. In this work, two different mixtures were prepared in fractions of 9:1 and 7:3. The results in Table III indicate that the $MPE \pm SPE$ is 5.9 ± 0.18 and 1.75 ± 0.05 for these mixtures. In another study [29], the dielectric properties of the mixture of DMSO and monohydric alcohol were analyzed. In this work, DMSO and ethanol mixture was prepared with a volume fraction of 2.3:7.7, corresponding to a molar fraction of 2:8. The results show that the $MPE \pm SPE$ is 8.9 ± 0.05 . Similarly, DMSO and 1-butanol mixture solution was prepared

with a volume fraction of 5.4:4.6, that is molar fraction of 6:4. The obtained results indicate $\text{MPE} \pm \text{SPE}$ of 4.83 ± 0.02 . Consequently, the results obtained from this work match well with the literature data, which were obtained through different methods.

As a final example, the trained NN is compared with the brute force look up table (LUT) approach. The LUT has two problems: (i) it requires a data table to be held in memory and (ii) for each estimation, the points that are close to the data point has to be determined, which requires evaluating the distance between the data point and the points in the LUT. These two problems become worse with increasing the dimension of the measured data. In contrast to this, a trained NN consists of simple computations (multiplications, summations and activation function evaluations). From another perspective, LUT is similar to memorization, it tries to separate all instances of data points by dividing the output space into Voronoi cells with respect to a metric, while NN is akin to generalization (or vary much similar to learning with aid of a complicated formula). The goal of NN is to find a nonlinear function that can map the input to output. To further explore the difference, the DMSO example in Table II is re-estimated with the LUT approach. 80% of the dataset (17732×0.8 S-parameters simulations, each of which includes 276 frequencies) are used to form a LUT. With the perspective defined above, we can think that there are 17732×0.8 many points in $R^{276 \times 2}$ in LUT. Then, the Euclidean distance between DMSO measurement in Table II and each data point in LUT is calculated and the Debye parameters of DMSO are assigned as the Debye parameters of the closest point in LUT. To assess the robustness of the LUT based method, it was evaluated 50 times (with different selections of 17732×0.8 many S-parameters simulations from 17732 simulations) and the average Debye parameters are estimated as $\epsilon_s = 48.7$, $\epsilon_\infty = 7.35$ and $\tau = 24.0$ ps with an MPE of 3.37 % (this was 1.21 % for DMSO using NN as seen from Table II). In terms of computational speed, NN based method spends 3.8 ms on average, while LUT spends 24.0 ms on average for one single dielectric property estimation. From the point-view of memory consumption, the LUT needs much more resources than the NN, since it needs a large table ($276 \times 17732 \times 0.8 + 3 \times 17732 \times 0.8 = 3.9 \times 10^6$ many complex numbers) to be held in memory to decide the best suitable estimation; while NN requires to hold the coefficients of designed network ($552 \times 128 + 128 \times 128 + 128 \times 128 + 128 \times 64 + 64 \times 3 = 1.2 \times 10^5$ many real number). In conclusion, the cost of using NN is to train a neural network, yet after training NN is more efficient than LUT approach both in terms of time and memory performance.

IV. CONCLUSION

In this work, an alternative approach is proposed for obtaining Debye parameters from the reflection coefficient response of the OECP when terminated with a material by utilizing a deep learning model. A synthetically generated dataset was used to design the deep learning model. The synthetic dataset was produced by modeling the OECP with the traditional

admittance model [14]. Theoretically modeling the OECP enabled us to effortlessly create a large-scale dataset utilized for designing the deep learning model. A combination of 29 ϵ_s , 12 ϵ_∞ and 51 τ Debye parameters were used to compose Debye models representing a wide range of materials. Among the generated Debye parameters 17732 samples were selected from the generated dataset and reflection coefficients were calculated from 0.5 to 6 GHz with 267 frequency points using the admittance model. A total number of 276×17732 input dataset (reflection coefficients) and 3×17732 output dataset (Debye parameters) was produced. To design the deep neural network, 80, 10, 10 % of the dataset was used for training, validating and testing the model, respectively. The model has (mean) $\pm$ (std.dev) percent relative errors between 1.86 ± 3.01 , 3.33 ± 9.52 and 2.07 ± 7.42 for predicting ϵ_s , ϵ_∞ and τ of test set (10% of the generated dataset), respectively. In order to test the designed deep learning model with experimental results, 625 input dataset (reflection coefficients) was prepared using measurements collected from five different standard liquids, four mixtures and a gel-like material. Collected measurements were performed in the frequency range of 0.5 to 6 GHz with 20 MHz resolution. The complex dielectric constants are obtained from the Debye parameters retrieved using the optimized deep learning model and the calculated complex permittivities were compared with reference data obtained from the literature. Obtained minimum and maximum (mean) $\pm$ (std.dev) complex permittivity percent relative errors are 1.21 ± 0.06 and 10.89 ± 0.08 , respectively.

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